

Supplementary information

Modelling human–natural systems interactions with implications for twenty-first-century warming

In the format provided by the authors and unedited

1 *Supplementary Information*
2 *for*

3
4 **Modeling human-natural systems interactions: Implications for 21st-century warming**
5 **trends**

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12 *Nature Sustainability*

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19 Part 1 (S1): Full technical description of ISEEC (Pages 1 to 19)

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21 Part 2 (S2): Sensitivity studies conducted with ISEEC (Pages 20 to 35)

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Part 1
Full technical description of ISEEC
including 2 supporting tables and 4 supporting figures

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50 **1. ISEEC Model Architecture**

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52 ISEEC consists of two coupled models: the Natural Systems Model (NSM) and the Social Systems Model
53 (SSM). Carbon emissions simulated by the SSM serve as an input to simulate CO₂ concentration and surface
54 temperature trends by the NSM. In turn, the simulated surface temperature trends from the NSM influence the
55 simulated primary energy and carbon emissions in the SSM via societal response to climate risks.

56 The single external input to ISEEC is global Gross Domestic Product (GDP). Using this input, ISEEC
57 estimates the total primary energy supply (TPES; hereafter referred to as primary energy, PE) needed to sustain the
58 economy and its growth, CO₂ emissions due to PE, warming due to CO₂ emissions, and societal actions in response
59 to the warming to reduce CO₂. Our primary focus is to illustrate socio-economic-energy-climate interactions
60 resulting from fossil fuel consumption. Towards this focused objective, we prescribe from published sources climate
61 forcing terms due to non-fossil sources, such as radiative forcing for non-CO₂ greenhouse gases, radiative forcing
62 due to aerosols that are also major sources of air pollution, and CO₂ emissions from land use and land changes (e.g.,
63 deforestation and biomass burning). However, a portion of the above non-CO₂ forcing terms are also emitted by
64 fossil fuels and we account for these forcings with fossil fuel use.

65 The model simulations begin in 1850 and extend to 2100. The SSM calculates the primary energy to
66 sustain the economy. For the historical period (up to 2015), the SSM adopts published values of primary energy and
67 simulates the relative fraction of fossil fuels and renewable sources. For the period beyond the present (starting from
68 2016), the SSM uses global GDP as an input to estimate primary energy, assuming future improvement of energy
69 intensity. Most importantly, it simulates the relative fraction of fossil fuels and renewable fuels that contribute to
70 primary energy. This relative fraction depends on societal, policy, and technological responses to the global
71 warming level, an output from by NSM component of ISEEC. The NSM uses CO₂ emissions calculated by the SSM
72 to simulate CO₂ atmospheric concentration as well as the radiative forcing due to CO₂ and the global warming level.

73 The novel aspects of ISEEC are the following:

74

75 **i. Two-way coupling between the social and natural systems.**

76 The primary energy and the shift from fossil fuels to renewables for PE are formulated to be dependent on
77 the *responses* of social/economic systems to observed warming. These responses include:

- 78 • Societal Response for climate actions based on scientific findings and observed data since climate change is
79 happening now and is emerging beyond the climate/weather noise.
- 80 • Policy Response in anticipation of or after Societal Response.
- 81 • Scaling up of existing technologies to meet policy mandates.
- 82 • Development of new carbon-free energy technologies¹.
- 83 • The scaling-up of these technologies worldwide also called Technology Diffusion.
- 84 • Start-up investment to boost the growth of new technologies.

85

86 **ii. Feedbacks between energy demands of atmospheric carbon extraction (ACE), cost of ACE, and warming.**

87 ISEEC estimates the amount of artificial extraction of CO₂ to generate the needed negative emission.
88 Following the strategy laid out in Fuss et al², the model treats three separate approaches for carbon extraction: 1)
89 extraction using land-based carbon sequestration by soil (charcoal) and afforestation; 2) extraction using
90 mineralization, algae, and biogeochemical modification; 3) direct air capture by mechanical and chemical extraction
91 of carbon. The growing capacity of ACE is constrained by technology development time and diffusion time, like
92 renewable energy technology. Additional constraints on the growing capacity of ACE include the cost of extraction
93 relative to a fraction of total GDP, which both vary with time, and the geophysical limits for storage of the extracted
94 CO₂ in terms of annual amount and cumulative amount. In contrast to Fuss et al., Field and Mach³ portray a more
95 cautious approach to negative emissions technology. ISEEC explicitly accounts for the PE used for ACE and its
96 potential offset to the net amount of carbon extraction if energy to power ACE is supplied from carbon-emitting
97 sources^{4,5}.

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99 **2. Natural system model (NSM)**

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101 NSM consists of two interacting components described next and in Table S1.

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Table S1. Governing equations and parameters for the carbon-climate model used in the Natural Systems Model of ISEEC (adopted from Sanderson et al., 2017⁶). Note that CO₂ emission E(t) in the carbon cycle model is calculated from the fossil fuel energy supply E_{II}(t) from the SSM (Table S2).

Climate Model	$\frac{\partial T_a(t)}{\partial t} = \frac{1}{\kappa_l} (5.35 * \ln\left(\frac{C_a(t)}{C_a(0)}\right) + F(t) - \lambda * T_a(t) - D_o * (T_a - T_o))$	(1.1)
	$\kappa_l = 20, \lambda = \frac{1}{0.8}, D_o = 0.4, C_a(0) = \frac{280}{\rho_a}$	
	$\frac{\partial T_o(t)}{\partial t} = \frac{1}{\kappa_o} * D_o * (T_a - T_o)$	(1.2)
	$\kappa_o = 20, D_o = 0.4$	
Carbon Cycle Model	$\frac{\partial C_a(t)}{\partial t} = \frac{E(t) - (\gamma_l + \gamma_o) * \frac{\partial T_a(t)}{\partial t} * (1 + \delta T_a)}{1 + \rho_a(\beta_l)} - \beta_o(\rho_a C_a - \rho_o C_o)$	(2.1)
	$\gamma_l = -0.13, \gamma_o = -0.2, \beta_o = 0.2, \rho_a = \frac{10^6}{1.8*10^{20}*12*10^{15}}, \rho_o = \frac{280}{100}, \delta = 1.1, \beta_l = 0.25$	
	$\frac{\partial C_o(t)}{\partial t} = \beta_o(\rho_a C_a - \rho_o C_o) + \gamma_o * \frac{\partial T_a(t)}{\partial t} * (1 + \delta T_a) - \beta_{od}(\rho_o C_o - \rho_{od} C_{od})$	(2.2)
	$\gamma_o = -0.2, \beta_o = 0.2, \rho_a = \frac{10^6}{1.8*10^{20}*12*10^{15}}, \rho_o = \frac{280}{100}, \beta_{od} = 0.25, \rho_{od} = \frac{280}{1000}, \delta = 1.1$	
	$\frac{\partial C_{od}(t)}{\partial t} = \beta_{od}(\rho_o C_o - \rho_{od} C_{od})$	(2.3)
	$\rho_o = \frac{280}{100}, \beta_{od} = 0.25, \rho_{od} = \frac{280}{1000}$	

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2.1 The coupled carbon-climate model

The CO₂ concentration is simulated with a carbon cycle model that considers land and ocean biological uptake and carbon diffusion into the surface ocean and deep ocean. The performance of this simpler carbon cycle

114 model has been validated against observations⁷ and the more comprehensive carbon cycle model (such as the one
 115 used in ref 8 and 9). The set-up of this carbon-cycle and energy balance model was detailed in ref 6 but we provide a
 116 brief overview of governing equations and their key parameters (Extended Data Table 2).

117 The core of the model is five differential equations about mass and energy conservation over time.

118 The first equation describes the evolution of the atmospheric temperature:

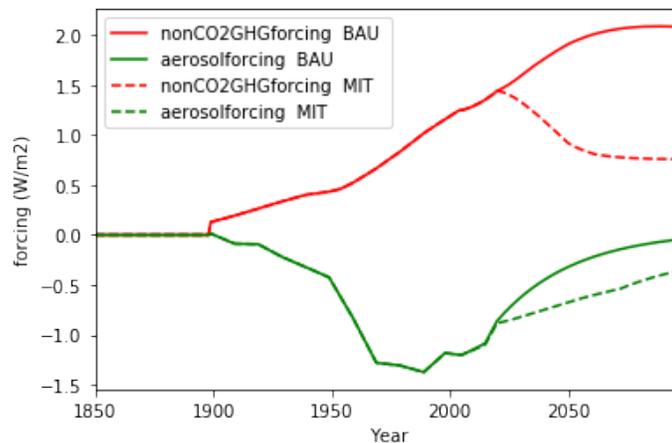
$$119 \frac{\partial T_a(t)}{\partial t} = \frac{1}{\kappa_1} \left(5.35 * \log \left(\frac{C_a(t)}{C_a(0)} \right) + F(t) - \lambda * T_a(t) - D_o * (T_a - T_o) \right) \quad (1)$$

121 where t is time and T_a and T_o are temperature anomalies of the atmosphere and ocean, respectively. The first part of
 122 the equation captures radiative forcing onto the surface-atmosphere system and the second part models heat transfers
 123 into the ocean.
 124

125 F(t) is the sum of all non-CO₂ forcing, which includes non-CO₂ gases and aerosols (Fig. S1-1). For cooling
 126 aerosols, such as sulfate and nitrate, we assume they will be reduced in the future regardless of scenarios due to air
 127 quality concerns. For warming aerosols (black carbon, which is also co-emitted with organic carbon) and other
 128 short-lived climate pollutants (SLCP), there are three different configurations in our model:

- 129 1. partially coupled with fossil fuel. Note in most cases, this implies reduction, but if fossil fuel usage
 130 increases as in some cases, SLCP will increase. For the portion of SLCP that is not coupled with fossil fuel
 131 use, we assume it will stay high.
- 132 2. without coupling, and assuming SLCP will stay high (i.e., leveling off at the 2030s). This is the BAU in
 133 Fig. S1-1.
- 134 3. without coupling and assuming SLCP will decrease quickly. This is the full mitigation as in Fig. S1-1.

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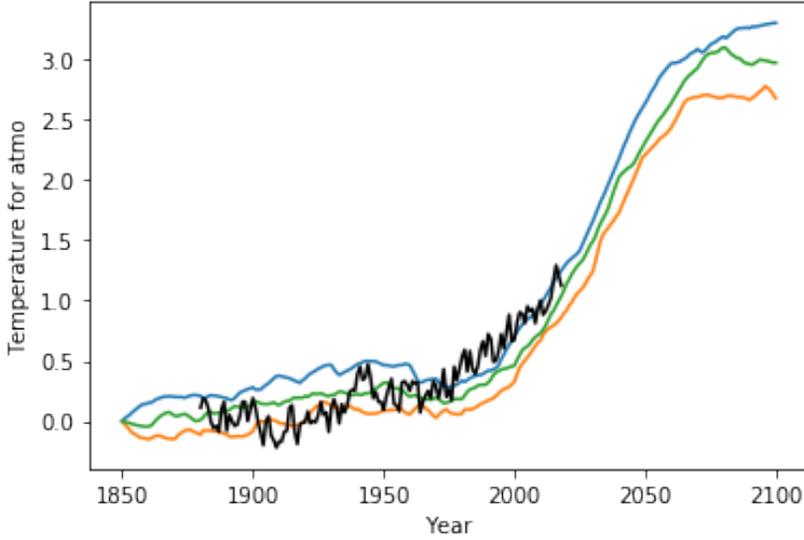
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138 **Fig. S1-1: non-CO₂ radiative forcing input to ISEEC under cases where the non-CO₂ species are not coupled**
 139 **to fossil fuel use. “BAU” stands for business as usual or baseline. “MIT” stands for full mitigation.**

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141 λ is the climate sensitivity parameter in $\text{Wm}^{-2}\text{K}^{-1}$. Our model can also mimic the probabilistic projection due
 142 to internal variability and the uncertain range of climate sensitivity. The coupled model results (Fig. S1-2) appear to
 143 be insensitive to the noise introduced, showing numerical stability with the default time step of one year.



144
 145 **Fig. S1-2. Comparison of ISEEC simulated temperature trend with observations. Blue and orange show**
 146 **maximum and minimum at each time step and green show the median estimates. Observations are from**
 147 **GISTEMP¹⁰.**

148
 149 κ_l is the thermal heat capacity of the land surface. C_a is the atmospheric carbon content in Pg. D_o is the
 150 thermal diffusion parameter between the atmosphere and the shallow ocean.

151
 152 The second equation describes the evolution of the atmospheric carbon content (in Pg C, not in ppm):

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$$\frac{\partial C_a(t)}{\partial t} = \frac{E(t) - (\gamma_l + \gamma_o) * \frac{\partial T_a(t)}{\partial t} * (1 + \delta T_a)}{1 + \rho_a * (\beta_l)} - \beta_o(\rho_a C_a - \rho_o C_o) \quad (2)$$

155
 156 The first part of the equation's right side is the land surface carbon responding to emission and the second
 157 part is the carbon diffusion into the ocean. $E(t)$ is the anthropogenic carbon emissions (which can also include
 158 negative emission sources) in Pg. γ_l and γ_o are the temperature-driven carbon feedbacks (in Pg K^{-1}) due to dissolved
 159 carbon in soil and seawater, both of which are negative values. ρ is a conversion factor from carbon content in Pg
 160 (i.e., Gt) to concentration in ppm, which has different values for the atmosphere, surface ocean, and deep ocean. β_l
 161 is the CO_2 fertilization parameter (i.e., carbon diffusion into land biosphere) and similarly, β_o is the carbon diffusion
 162 parameter from the atmosphere to the ocean.

163 The third and fourth equations describe carbon concentration in the ocean:

164

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$$\frac{\partial C_o(t)}{\partial t} = \beta_o(\rho_a C_a - \rho_o C_o) + \gamma_o * \frac{\partial T_a(t)}{\partial t} * (1 + \delta T_a) - \beta_{od}(\rho_o C_o - \rho_{od} C_{od}) \quad (3)$$

166
$$\frac{\partial C_{od}(t)}{\partial t} = \beta_{od}(\rho_o C_o - \rho_{od} C_{od}) \quad (4)$$

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168 In Eqn. 3, change in the carbon content of the shallow ocean can be due to three terms: $\beta_o(\rho_a C_a - \rho_o C_o)$
 169 measures carbon diffusion from the atmosphere to the shallow ocean; γ_o measures ocean carbon storage sensitivity
 170 due to temperature change (both in warming rate as well as the anomaly), which is a negative value due to degassing
 171 of the warmer ocean; and $\beta_{od}(\rho_o C_o - \rho_{od} C_{od})$ measures carbon transfers into the deep ocean. In Eqn. 4, the carbon
 172 storage in the deep ocean all comes from the shallow ocean.

173 The last equation governs the change in ocean temperature over time:

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$$\frac{\partial T_o(t)}{\partial t} = \frac{1}{\kappa_o} * D_o * (T_a - T_o) \quad (5)$$

176

177 The heat flux affecting ocean temperature comes from diffusion from the atmosphere, and κ_o is the ocean
 178 heat capacity.

179

180 Lastly, we provide a quick summary of the key parameters in this simple carbon-climate model:

- 181 • λ is the climate feedback parameter and denotes the sum of the radiation energy emitted and reflected to
 182 space per degree of warming. For λ , we adopt the value of $1.25 \text{ Wm}^{-2} \text{ } ^\circ\text{C}^{-1}$) which is consistent with a
 183 climate sensitivity of 4°C per doubling of CO_2 concentration.
- 184 • κ is the heat capacity, the larger the κ , the longer it will take to warm.
- 185 • β is the carbon diffusion coefficient (Pg/ppm), the larger the β , the carbon transfer into ocean/land more
 186 easily given the same difference in mixing ratio.
- 187 • γ is the carbon content sensitivity to temperature rise (Pg/ $^\circ\text{C}$).

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189 **3. Social Systems Model (SSM)**

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191 SSM consists of a set of interacting components described next. The governing equations are written down
 192 in Table S2.

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Table S2. Governing equations and parameters for the Social Systems Model of ISEEC

Definitions	Equations
<p>PE: total primary energy supply</p> <p>r_{EI}: a ratio representing the reduction of Energy Intensity due to climate actions</p> <p>GDP: global gross domestic product taken from published sources</p>	<p>$PE(t) = r_{EI}(T(t)) * EI(t) * GDP(t) * \sum_{i=1}^n \sum_{j=1}^k E_{ij}(t)$ with the constraint that $\sum_{i=1}^n \sum_{j=1}^k E_{ij}(t) = 1.0$; $n=2$ and $k=4$</p> <p>E_{ij} Fractional contributions from the various energy sources $i=1$: CO₂ emitting energy sources; $j=1$ is fossil fuels; $j=2$ is traditional biomass. $i=2$: various renewable sources.</p> <p>E_{21} and E_{22} are detailed in the rows 2 and 3 below.</p> <p>E_{23} is traditional nuclear; and E_{24} is hydro and geothermal</p> <p>$r_{EI}(t) = 1$ for $t < 2015$; and $r_{EI}(t) = e^{-0.005 * T * (t - 2015)}$ for $t \geq 2015$</p>
<p>E_{21}: Renewable Energy- Off-the-shelf technologies</p> <p>τ_{21}^R: societal response time</p> <p>τ_{21}^P: policy response time</p> <p>τ_{21}^{DV}: tech Development time</p> <p>τ_{21}^{DF}: tech Diffusion time</p> <p>η_{21}: startup term</p>	<p>$\frac{dE_{21}}{dt} = \left[1 - \frac{E_{21}(t)}{k_{21}} \right] * \left[\frac{E_{21}(t)}{\tau_{21}(t)} \right] + \eta_{21}$</p> <p>$\tau_{21} = \tau_{21}^{R \rightarrow P} + \tau_{21}^{DV} + \tau_{21}^{DF}$</p> <p>$\tau_{21}^{R \rightarrow P} = \max(\tau_{21}^R, \tau_{21}^P)$</p> <p>$\tau_{21}^R = \tau_{21}^R(0)e^{-a_1 T}$; $\tau_{21}^R(0) = 50$, $a_1 = 2$;</p> <p>$\tau_{21}^P = \frac{\tau_{21}^R}{2}$; $\tau_{21}^{DV} = 0.0$; $\tau_{21}^{DF} = \frac{b_1}{1 + b_2 T^2}$; $b_1 = 25$; $b_2 = 2$</p> <p>$\eta_{21} = \eta_0 - \frac{E_{21}(t)}{\tau_{21}(t)}$; If $\eta_{21} < 0$; set $\eta_{21} = 0$;</p> <p>$\eta_0(t > 1950) = 0.1\%/year$; $\eta_0(t < 1950) = 0$;</p> <p>$k_{21} = 65\%$</p>
<p>E_{22}: Renewable Energy- New technologies</p>	<p>$\frac{dE_{22}}{dt} = \left[1 - \frac{E_{22}(t)}{k_{22}(t)} \right] * \left[\frac{E_{22}(t)}{\tau_{22}(t)} \right] + \eta_{22}$</p> <p>$\tau_{22} = \tau_{22}^{R \rightarrow P} + \tau_{22}^{DV} + \tau_{22}^{DF}$</p> <p>$\tau_{22}^{DV} = \frac{\tau_0^{DV}}{(1+T)^{n_{22}^{DV}}}$; ($\tau_0^{DV} = 30$, $n_{22}^{DV} = 2$)</p> <p>$k_{22}(t) = 1 - E_{12}(t) - E_{21}(t) - E_{23}(t) - E_{24}(t)$</p> <p>$\eta_{22} = \left\{ \eta_0 - \frac{E_{22}}{\tau_{22}} \right\}$; if $\eta_{22} < 0$; set $\eta_{22} = 0.0$;</p> <p>$\eta_0(t > 2016) = 0.1\%/year$; $\eta_0(t < 2016) = 0$</p>
<p>Atmospheric Carbon Extraction (details in Supplementary Information Part 1, Section 3.4)</p> <p>C_i: CO₂ extracted in Gt/year.</p> <p>C_1 denotes extraction through afforestation and enhancement of soil</p>	<p>$\frac{dC_i}{dt} = \varphi_i * \alpha_i * \gamma_i * \left(\frac{C_i(t)}{\tau_i(t)} \right) + \eta_i - \beta_i$</p> <p>$\varphi_i = \left[1 - \frac{\sum_{j=0}^t C_j}{K_i} \right]$; $k_1 \& k_2 = 500$ Gt; $k_3 = 5000$ Gt</p> <p>$\alpha_i = \left[1 - \frac{C_i}{L_i} \right]$; $L_1 = L_2 = 4$ Gt CO₂/year; $L_3 = 20$ Gt CO₂/year</p> <p>$\gamma_1 = \gamma_2 = 1$; $\gamma_3 = 1 - \frac{Cost_3(t)}{f_{GDP}(t) * GDP(t)}$</p>

<p>carbon extraction; C_2 denotes extraction by mineralization and algae production in oceans; C_3 is direct air capture.</p> <p>φ_i: limiting factor for the cumulative extraction potential</p> <p>α_i: limiting factor for the annual extraction potential</p> <p>γ_3: limiting factor due to the cost exceeding a certain percentage of GDP</p> <p>η_i: initial investment to jump start the diffusion</p> <p>$\tau_i(t)$: the response times</p> <p>β_i: the release of CO_2 due to the fossil fuel related energy consumed by the carbon removal technologies</p> <p>e_i: energy needed to extract a unit mass of CO_2</p> <p>$f_i(t)$: fossil fuel fraction of the energy used</p> <p>$\rho_i(t)$: carbon intensity</p>	<p>$\text{Cost}_3(t) = C_3(t) * \text{CPT}_3(t)$</p> <p>$\text{CPT}_3$ (Cost Per Ton) = $\frac{500}{1 + 2 * C_3(t)}$; if $\text{CPT} < 50$, set $\text{CPT} = 50$</p> <p>$f_{\text{GDP}}(t) = 0.5\% * T^2$</p> <p>$\tau_i(t) = \tau_i^0 e^{-c_0\{T(t)-\alpha_i\}}$ ($\tau_{i=1 \text{ to } 3}^0 = 10$; $c_0 = 1$; $\alpha_1 = 1 \text{ }^\circ\text{C}$; $\alpha_2 = 1.5 \text{ }^\circ\text{C}$; $\alpha_3 = 2 \text{ }^\circ\text{C}$;</p> <p>$\eta_i = \{\eta_0 - \frac{c_i}{\tau_i}\}$; $\eta_0 = 0.001 \text{ Gt CO}_2/\text{year}$</p> <p>If η_i is less than zero, set it to be zero.</p> <p>$\beta_i = \frac{C_i * e_i * f_i * \rho_i}{\tau_i}$</p> <p>$e_1 = e_2 = 0$; $e_3 = 10 \frac{\text{EJ}}{\text{GtCO}_2}$,</p> <p>$f_i = E_{11}(t)$</p> <p>$\rho_i(t)$ decrease from 83 to 72 gCO_2/MJ when T increases from 1 to 2$^\circ\text{C}$ (details in Section 3.3)</p>
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199 **3.1 PE from non-renewable and renewable sources**

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 201 Non-renewable sources are fossil fuels and non-renewable biomass (e.g., deforestation and the burning of
 202 biomass for PE). Renewable sources include solar, wind, nuclear, hydrogen from solar-powered electrolysis,
 203 hydropower, and geothermal.

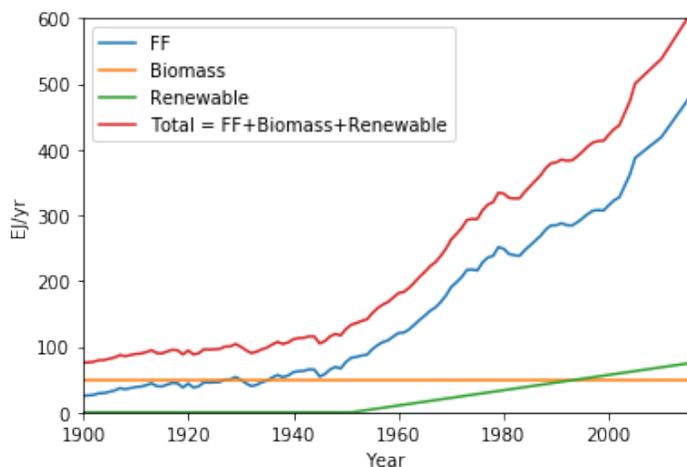
204 Let $\varepsilon_T(t)$ be the global total PE per year. We can express $\varepsilon_T(t)$ as

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 206
$$\varepsilon_T(t) = r_{EI}(t) * \varepsilon_{baseline}(t) * \sum_{i=1}^n \sum_{j=1}^k E_{ij}(t) \tag{6}$$

207
 208 where $\varepsilon_{baseline}(t)$ is the baseline global PE (EJ/year), which is the major external input to the model.

209 For the historical period (1850-2015), we adopted $\varepsilon_{baseline}(t)$ directly from published sources¹¹, with the
 210 fossil fuel energy largely consistent with published CO₂ emission inventory¹². Biomass-burning energy makes up
 211 8% of the total in 2015. Renewable energy capacity makes up 12% of the total in 2015. Note that for the historical
 212 period, the constructed PE is the only external input to the model, while the fractional contribution of fossil fuel,
 213 biomass, and various renewable sources are all simulated by the model and are validated with the published datasets
 214 (Fig. 3 in the main text).

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216
 217 **Fig. S1-3. Total PE breakdown in the simulated historical period.**

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 219 For the future period (2016 - 2100), we adopted the GDP outlook¹³ under a baseline scenario (SSP585;
 220 Extended Data Figure 1), which assumes a rapid economic growth with high energy demand (despite slower
 221 population growth).

222 The PE is then calculated by assuming a 2.5%/year reduction in energy intensity (i.e., PE/GDP) from its
 223 current value of 7 EJ/Trillion USD before 2040, and a 1.3%/year reduction in energy intensity after 2040, all
 224 consistent with SSP5 assumptions (Extended Data Figure 1b). The primary energy throughout the model simulation
 225 period (1850–2100) is shown for reference, which serves as a major input to the SSM.

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$E_{ij}(t)$ is the *fractional contribution to the primary energy from the various energy sources*, denoted by the indices i and j .

- Index $i=1$ denotes traditional energy sources (fossil fuel and biomass); and $i=2$ denotes non-CO₂ emitting energy sources including various renewables. CO₂ emissions can then be obtained by partitioning the fossil-fuel-related emissions ($i=1$) from other zero-emission clean sources ($i=2$).
- Index j denotes the various sectors or sub-sources (for example, wind, solar, geothermal, nuclear, hydropower, etc.) within each category of the index i .

It should be noted that, by definition,

$$\sum_{i=1}^n \sum_{j=1}^k E_{ij}(t) \equiv 1.0$$
$$\text{so } \varepsilon_T(t) = r_{EI}(t) * \varepsilon_{baseline}(t) \tag{7}$$

Overall, we propose that societal response to climate disruption will tend to reduce CO₂ emissions in the following ways:

1. By reducing the energy intensity of the economy *beyond* that has been assumed in the baseline, by at least another 0.5%/year. If the energy intensity further improves by the societal response to climate disruption, the ratio $r_{EI}(t)$ would become less than 1. The EI reduction can be accomplished by improving the energy efficiency of end-use, reducing waste in transmission, reducing energy demand through lifestyle change, increasing the contribution of the shared economy, among other options. We cap the maximum reduction at 30% off the baseline EI, which is typically reached in the mid-21st century in our cases (see the difference between gross energy (GE) and adjusted GE in Fig. 4).
2. By reducing the carbon intensity of fossil fuel-based PE from 83 to 72 Gt CO₂/EJ throughout global warming transition from 1°C to 2°C. The potential reduction of the carbon intensity of fossil fuel energy can be accomplished by fuel switching from coal to gasoline and natural gas, among other options¹⁴.
3. While (1) and (2) above will reduce emissions from fossil fuels, the effects are rather limited (15% to 30% cut off the baseline emission). The more fundamental way of decarbonization is by replacing fossil fuel energy sources (E_{i1} term) with carbon-free sources (various E_2 terms)¹⁵. Next, we formulate the evolving capacity of renewables by coupling the growth rates of various clean energy sources with the societal responses to climate risks. These formulations are explained in detail in the following sub-sections.

3.1.1 CO₂ emitting sources: $i = 1$; $j = 1$ to 2

$j = 1$ denotes the fossil fuel source, such as gas, oil, and coal.
 $j = 2$ denotes other traditional sources of PE, such as traditional biofuel (e.g., firewood burning) and biomass burning power supply.

262 Note again, in Eqn. 1, $E_{11}(t)$ is fossil fuel PE in *relative* terms, not absolute values. From Eqn. 1, the PE
 263 due to CO₂-emitting sources is expressed as:

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$$265 \quad E_{11}(t) + E_{12}(t) = 1 - \sum_{i=2}^n \sum_{j=1}^k E_{ij}(t) \quad (8)$$

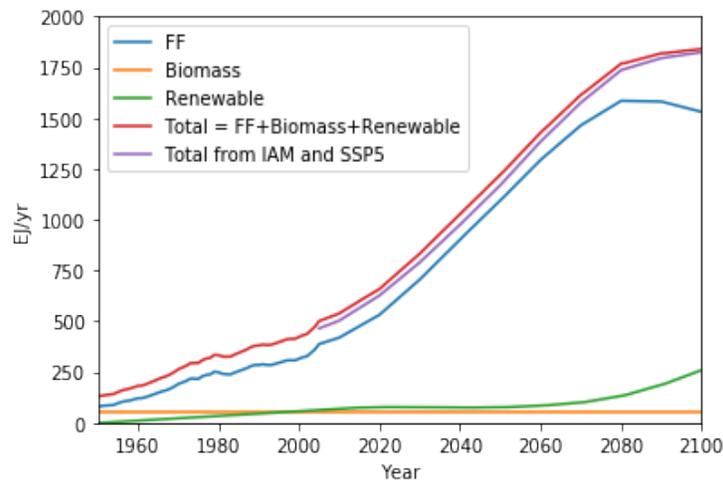
266

267 where the left side is the fractional PE due to CO₂ emitting sources and the right side is the difference
 268 between primary energy and PE from clean sources. Note that the total share of primary energy is 1.0 since all the
 269 $E_{ij}(t)$ terms make up the primary energy, $\varepsilon_T(t)$. For example, in order to reach zero carbon emissions (gross zero,
 270 not net-zero due to negative emission technology), the right side must be zero. That is, all PE is from renewable
 271 sources, which do not emit CO₂.

272 We use a few governing equations (see descriptions later) in ISEEC to simulate the historical and future
 273 evolution of E_{11} , formulated as a societal response to climate change. The historical and recent changes can be
 274 cross-validated with various published data sets (Fig. 2a in the main text). The fossil fuel CO₂ emissions will then be
 275 estimated from $E_{11}(t)$, using carbon intensity (CO₂ emission per fossil fuel-based PE) that gradually decreases with
 276 time. We then validate the simulated CO₂ emission from E_{11} by comparing it with CO₂ emission from the Global
 277 Carbon Budget (up to 2019). Simulated CO₂ emissions are within 10% of published values (Fig. 2b in the main
 278 text).

279 Note that $E_{12}(t)$ is the fractional PE from non-fossil fuel sources (e.g., traditional biomass burning for
 280 cooking, lighting, and heating by the world's poorest population). The projected values do not change much in the
 281 SSP5 future (yellow line of Fig. S1-4). Therefore, the absolute value, i.e., $\varepsilon_T(t) * E_{12}(t)$, in 2016 is held constant
 282 through 2100.

283



284
 285 **Fig. S1-4. Breakdown of total PE. Same as Fig. S1-3, but also including future period following SSP5-8.5.**

286

287 Thus, for years beyond 2016, $E_{12}(t)$, defined as the fraction of total, will actually decrease, because of the
 288 increase in primary energy:

289

$$E_{12}(t > 2016) = \frac{\varepsilon_T(2016) * E_{12}(2016)}{\varepsilon_T(t > 2016)} \quad (9)$$

291

292 Note that the emission-related to the E_{12} category has been included in Global Carbon Project as falling
293 under the land use (LU) category, which also implicitly includes the reduction of carbon sink due to deforestation
294 and land clearance. Thus, we directly prescribe the LU emission from published sources (Global Carbon Project
295 before 2019¹⁶ and SSP5-RCP8.5 after 2019¹⁷), without explicitly simulating LU-related CO₂ emission, which is a
296 subject of previous studies coupling climate and land use in the future¹⁸.

297 In summary, the anthropogenic CO₂ emission that leads to concentration increase is from sources of fossil
298 fuel (simulated E_{11} term) and land use (prescribed). The main contribution of ISEEC is to make E_{11} (via various E_{2j}
299 terms, defined in the next section) dependent on societal response to climate change. While E_{12} is included in the PE
300 but not explicitly accounted for in the carbon emission budget, it does not affect our findings since this study focuses
301 on future climate mitigation by reducing fossil fuels.

302

303 **3.1.2 Renewable Sources: $i = 2$; $j = 1$ to 4**

304

305 We consider the following categories of carbon-free energy sources:

- 306 • E_{21} is renewable energy using off-the-shelf technology, such as photovoltaics; wind; biofuels. No
307 development is needed for this category.
- 308 • E_{22} is renewable energy using emerging new technology, such as hydrogen from electrolysis, reusable
309 batteries, safe nuclear, micro-, and nano- grids. E_{22} is approximately zero as of 2016.
- 310 • E_{23} is traditional nuclear.
- 311 • E_{24} is traditional renewable energy, such as geothermal and hydropower, which are subject to geophysical
312 limitations.

313

314 From REN (2019) report¹⁹, for the year 2016, which is the start year of our “future” simulation:

- 315 • $E_{11} = 79\%$
- 316 • $E_{12} = 8\%$ (traditional non-renewable biomass)
- 317 • $E_{21} = 2.6\%$ (e.g., solar and wind)
- 318 • $E_{23} = 2.2\%$ (e.g., nuclear)
- 319 • $E_{24} = 7.8\%$ from geothermal (4.1%) and hydropower (3.7%)

320

321 Thus, we deduce that E_{22} is negligible, but we assume it to be 0.4% for emerging renewable technologies
322 (calculated as a residual of $1 - E_{11} - E_{12} - E_{21} - E_{23} - E_{24}$) as of 2016, which provides the initial condition for E_{22} in the
323 simulations.

324 Note that for the terms above, E_{21} (solar and wind) is the only one that will be simulated for a historical
 325 period (up to 2015), while E_{22} , E_{23} , and E_{24} are prescribed up to 2015 based on the reported present-day capacity
 326 (assuming linear growth starting from 2010, 1970, 1950, respectively). Thus, we first describe the treatment of the
 327 E_{21} term in detail below.

328

329 3.1.2.1 E21: Renewable Sources Using Current Technologies

330

331 We develop the equation for the first renewable term: E_{21} (renewable using current technology, such as
 332 solar and wind).

333

334
$$\frac{dE_{21}}{dt} = \text{Startup} + \text{Diffusion, in which} \quad (10)$$

335 Startup: $\eta_{21} = \{\eta_0 - \frac{E_{21}(t)}{\tau_{21}(t)}\}$; if $\eta_{21} < 0$; set $\eta_{21} = 0$

336

337 Diffusion = $\left[1 - \frac{E_{21}(t)}{k_{21}}\right] * \left[\frac{E_{21}(t)}{\tau_{21}(t)}\right]$

338

339 τ_{21} is effective Response Time in years.

340
$$\tau_{21} = \tau_{21}^{R \rightarrow P} + \tau_{21}^{DV} + \tau_{21}^{DF} \quad (11)$$

341 in which

342 $\tau_{21}^{R \rightarrow P}$: the combined response to societal response and policy response

343 τ_{21}^R : societal response time

344 τ_{21}^P : policy response time

345 τ_{21}^{DV} : technology development time

346 τ_{21}^{DF} : technology diffusion time

347

348 For the standard model, we assume that it is the larger of the two response times, that is $\max(\tau_{21}^R, \tau_{21}^P)$. For

349 an upper range of response time, we assume $\tau_{21}^{R \rightarrow P} = \tau_{21}^R + \tau_{21}^P$.

350 Each of the response times is expressed as a function of warming as follows

351

352
$$\tau_{21}^R = \tau_{21}^R(0) e^{-a_1 T} \quad (12)$$

353 In which, $\tau_{21}^R(0) = 50$, $a_1 = 2.0$

354
$$\tau_{21}^P = \frac{\tau_{21}^R}{a_2}, \quad \text{in which, } a_2 = 2.0 \quad (13)$$

355 $\tau_{21}^{DV} = 0.0$ because E_{21} -related renewable technology is already developed as of 2016.

356
$$\tau_{21}^{DF} = \frac{b_1}{1 + b_2 T^2} \quad (14)$$

357 in which, $b_1 = 25$, $b_2 = 2 \quad (15)$

358

359 The $\frac{E_{21}}{k_{21}}$ term within the square bracket limits the growth of E_{21} fraction to the total energy. This can come
360 from limitations of land area, battery waste, etc.

361 We set $k_{21}=0.65$ (16)

362 That is, conventional solar and wind can only meet 65% of the primary energy at maximum.

363 In summary, with Eqn. 10, we can integrate $\varepsilon_T(t) * E_{21}$ from 0 in the year 1850, continually through 2100,
364 thus achieving the full coupling of energy-emission-climate. The startup term, η_{21} , is the initial capacity building or
365 investment needed to prime (jump-start) the diffusion. Initially, E_{21} is zero and as can be inferred from Eqns. 3 to 5,
366 $\frac{dE_{21}}{dt}$ is determined by η_0 , which is set to 0.1%/year. The diffusion term allows for the diffusion of technology, past
367 the initial stage, to its full potential, which is determined by k_{21} . The variable k_{21} is the upper limit (the full potential)
368 for the percentage of PE that can be provided by E_{21} .

369

370 3.1.2.2 E_{22} : Renewable Using New Technology

371

$$372 \frac{dE_{22}}{dt} = \left[1 - \frac{E_{22}(t)}{k_{22}}\right] * \left[\frac{E_{22}(t)}{\tau_{22}(t)}\right] + \eta_{22} \quad (17)$$

$$373 \tau_{22} = \tau_{22}^{R \rightarrow P} + \tau_{22}^{DV} + \tau_{22}^{DF} \quad (18)$$

374 $\tau_{21}^R, \tau_{21}^P, \tau_{21}^{DF}$ are formulated the same as those for E_{21} .

$$375 \tau_{22}^{DV} = \frac{\tau_0^{DV}}{(1+T)^{n_{22}^{DV}}} \quad (19)$$

$$376 \tau_0^{DV} = 30$$

$$377 n_{22}^{DV} = 2$$

$$378 \text{If } \tau_{DV} < \tau_{DV}^{\min}; \tau_{DV} = \tau_{DV}^{\min} = 4$$

379

$$380 k_{22}(t) = 1.0 - E_{12}(t) - k_{21} - E_{23}(t) - E_{24}(t) \quad (20)$$

381

382 As of 2016, $E_{23} = 0.02$; $E_{24} = 0.08$. So, with the assumed $k_{21}=0.65$, we set $k_{22} = 0.25$ in 2016 with the
383 expectation it will increase in future.

384

$$385 \eta_{22} = \left\{ \eta_0 - \frac{E_{22}}{\tau_{22}} \right\} \quad (\eta_0 = 0.1 \%), \text{ which is akin to } \eta_{21}.$$

386

387 The governing equation for E_{22} (Eqn. 17) is only used for future projection. Without the start-up term, it
388 will take several decades for a technology to diffuse from zero to its full potential. For the historical period, since E_{22}
389 $= 0.4\%$ in 2016, we assume that $\varepsilon_T(t) * E_{22}$ increases linearly from 0 in 2000 to its 2016 value.

390

391 3.1.2.3 E_{23} : Traditional Nuclear

392

393 For the historical period, since $E_{23} = 2.2\%$ in 2016, we assume that $\varepsilon_T(t) * E_{23}$ increases linearly from 0 in
394 1970 to its 2016 value. For the future, we keep the PE in absolute value (not the fraction) the same as 2016. As a
395 result, E_{23} , defined below as a fraction, will gradually decrease.

396

$$397 \quad E_{23}(t>2016) = \frac{\varepsilon_T(t) * (2016) * E_{23}(2016)}{\varepsilon(t>2016)} \quad (21)$$

398

399 **3.1.2.4 E_{24} : Traditional Renewable Sources (geothermal, hydropower)**

400

401 For the historical period, since $E_{24} = 7.8\%$ in 2016, we assume $\varepsilon_T(t) * E_{24}$ increases linearly from 0 in 1950
402 to its 2016 value. For the future, we keep the PE in absolute value (not the fraction) the same as 2016. So E_{24} ,
403 defined below as a fraction, will gradually decrease.

404

$$405 \quad E_{24}(t>2016) = \frac{\varepsilon_T(t) * (2016) * E_{24}(2016)}{\varepsilon(t>2016)} \quad (22)$$

406 **3.2 Mitigation due to Improvements in Energy Intensity**

407

408 The baseline primary energy, $\varepsilon_{baseline}(t)$, assumes implicitly a marginal 1.3-2.5% per year decrease in
409 energy intensity. However, previous studies²⁰ suggest a further decrease of up to 1.4% per year in energy intensity is
410 possible²¹.

411 $r_{EI}(t)$ represents the *ratio* of the energy intensity (EI, primary energy per GDP, in the unit of
412 EJ/TrillionUSD) between the actual world and the baseline scenario. We propose that

413

$$414 \quad r_{EI}(t) = \frac{EI(t)}{EI_{baseline}(t)} = e^{-0.005 * T * (t-2015)} \quad \text{for } t \geq 2015 \quad (23)$$

$$415 \quad \text{With the constraint that } r_{EI} > 0.7 \quad (24)$$

416

417 The temperature parameterization assumes that as the planet warms there will be more incentive to achieve
418 a stronger reduction in energy intensity and the percent reduction is 0.5-2.0% per year, in addition to the assumed
419 reduction in energy intensity in the $EI_{baseline}(t)$. However, we limited the maximum feasible reduction in intensity
420 to be 30%, which is typically reached around 2050 in our base case, and it effectively translates to an *additional*
421 1.1%/year decrease during 2016 and 2050.

422 **3.3 Mitigation due to Improvements in Carbon Intensity**

423

424 Once we determine the primary PE from fossil fuels (E_{11} term), we use a carbon intensity factor to convert
 425 it to CO₂ emissions. This factor can be estimated from the published CO₂ emission and energy data and is dependent
 426 on the apportionment of fossil fuels between coal, oil, and natural gas. For example, switching from coal to oil and
 427 natural gas in the next few decades over part of the globe will reduce the carbon intensity. To factor this in without
 428 simulating the detailed makeup of fossil fuel, we propose that there will be a switch from coal to gasoline and gas
 429 when the warming exceeds 1.5°C. We mimic this transition by formulizing the following:

430 When T is less than 1°C, we adopt the carbon intensity of 83 gCO₂/MJ due to the current use of
 431 coal/gasoline/natural gas (2006-2015). When T is greater than 2°C, coal will be completely phased out, and we adopt
 432 a lower carbon intensity of 72 gCO₂/MJ. We assume a linear reduction of emission factor (i.e., carbon intensity)
 433 when T increases from 1 to 2 °C.

434

435 3.4 Atmospheric Carbon Extraction (ACE)

436

437 Let CO₂ extraction be denoted by C_i , typically shown in the unit of Gt CO₂ per year. We want to develop an
 438 equation for CO₂ reduction due to various ACE methods. The index i represents the approach of carbon extraction:

- 439
- $i=1$ denotes extraction using soil improvement, afforestation, and other land-based natural solutions.
 - $i=2$ denotes mineralization, algae, and biogeochemical modification.
 - $i=3$ denotes the mechanical-chemical extraction of carbon dioxide (i.e., direct air capture).

442

443 We make a clear distinction between gross extraction and net extraction, with the difference being
 444 emissions due to energy demand for powering ACE.

$$445 \frac{dGrossC_i}{dt} = \varphi_i * \alpha_i * \gamma_i * \frac{GrossC_i(t)}{\tau_i(t)} + \eta_i \quad \text{for } t > 2016 \text{ only.} \quad (25)$$

$$446 \frac{dNetC_i}{dt} = \frac{dGrossC_i}{dt} - \beta_i \quad \text{for } t > 2016 \text{ only.}$$

447 The first term on the right side is the limiting factor for the cumulative extraction potential and is defined
 448 as:

449

$$450 \varphi_i = \left[1 - \frac{\sum_{2016}^{t_n} \Delta t * NetC_i}{k_i} \right] \quad (26)$$

451

452 $\sum_{2016}^{t_n} \Delta t * C_i(t)$ is the cumulative net extraction from 2016 to a future year, t_n . Δt is the time step (1 year)
 453 such that the cumulative sum of the product is Gt CO₂ removed.

454 The rate-limiting factors, k_i , are:

455

$$456 k_1 = k_2 = 500 \text{ Gt CO}_2. \quad (27)$$

$$457 k_3 = 5000 \text{ Gt CO}_2.$$

458

459 While k_3 makes an almost limitless potential for $i=3$, the chemical and mechanical extraction is limited by
 460 annual extraction potential. This is treated in the second term α_i , a limiting factor defined as:

$$461 \quad \alpha_i = \left[1 - \frac{NetC_i}{L_i} \right]$$

462 The rate-limiting factors of L_i are:

$$463 \quad L_1 = L_2 = 4 \text{ Gt CO}_2/\text{year.} \quad (28)$$

$$464 \quad L_3 = 20 \text{ Gt CO}_2/\text{year}$$

465
 466 The third term is the economic limiting factor due to the ACE cost exceeding a certain percentage of global
 467 GDP. It is formulated as:

$$468 \quad \gamma_i = 1 \quad \text{for } i=1 \text{ and } 2.$$

$$469 \quad \gamma_3 = 1 - \frac{Cost_3(t)}{f_{GDP}(t) * GDP(t)} \quad (29)$$

470 where $Cost_3$ is estimated as:

$$471 \quad Cost_3 = NetC_3(t) * CPT_3(t) \quad (30)$$

472 where CPT_3 is the Cost Per Ton of CO_2 . Smith et al.²² estimated a range of \$1,650 to \$2,100 per ton of
 473 carbon, which translates to a CPT_3 of \$435 to \$572. We assume the central value of \$500 for CPT_3 in 2020, which
 474 would decrease in time because of the scale of the economy. We model it by letting:

$$475 \quad CPT_3(t) = \frac{500}{1 + 2 * NetC_3(t)}; \text{ where } NetC_3 \text{ is in the unit of Gt CO}_2/\text{year}$$

476 if $CPT_3 < \$50$, we set $CPT_3 = \$50$.

$$477 \quad f_{GDP}(t) = 0.5\% * T^2 \quad (31)$$

478
 479 GDP(t) is the GDP data obtained from SSP5, the highest growth among the five scenarios, for which we fit
 480 with an exponential function.

481
 482 The expression for $f_{GDP}(t)$ implies that societies' willingness to pay will depend on the magnitude of the
 483 warming. For example, when the warming reaches 1°C, the society will be willing to pay a maximum of 0.5% of the
 484 GDP; when the warming reaches 2°C, the society may be willing to pay 2% of GDP. In our base case, the ACE₃ cost
 485 amounts to 1.3% of GDP at most.

486 Our estimate of the cost is conservative. For example, we are ignoring the additional cost and energy
 487 incurred for storing the extracted CO_2 . For ACE₃, we need to store the extracted CO_2 in deep geological spaces (e.g.,
 488 regions where fossil fuels were extracted). To give a perspective on the magnitude of 600 billion tons, which is the
 489 estimated amount of CO_2 that would need to be stored from the fully coupled ISEEC (Fig. S1-1), the annual solid
 490 waste supply by the world is 2 billion tons, so we would need to create enough space to store 300 years' worth of
 491 solid waste. Therefore, in the sub-model, the ACE₃ capacity is also capped based on assumed geophysical limits for
 492 storage of the extracted CO_2 in terms of annual amount and cumulative amount.

493

494 We set $\text{NetC}_{i=1,2,3}(2016) = 0.0$ Gt/year, which will make it as an initial value problem. To avoid that,
 495 similar to the E_{21} formulation, we introduce a η_i term:

496
 497
$$\eta_i = \eta_0 - \frac{\text{GrossC}_i}{\tau_i} \quad (32)$$

498 We set $\eta_0 = 0.001$, but also tested 0.01 and 0.05

499 Note that if $\eta_i < 0$, we set $\eta_i = 0$ (33)

500
 501 The last term on the right side is CO_2 emission due to fossil fuel use by carbon removal technologies. It is
 502 expressed as:

503
 504
$$\beta_i = \frac{\text{GrossC}_i * e_i * f_i * \rho_i}{\tau_i} \quad (34)$$

505 Where, e_i is energy per ton of CO_2 extracted (in gross term).

506 For $i=1$ & $i=2$, we ignore the emission by setting $e_i = 0.0$, and thus $\beta_i = 0$ (35)

507 For $i=3$, Keith et al.²³ gives 8.81 GJ (using natural gas) per ton of gross extracted CO_2 . A literature review
 508 by Smith et al.²² gives 45 GJ per ton of carbon, which translates to 12.25 GJ/ton of CO_2 .

509 Therefore, here we adopt the estimates that

510 $e_3 = 10$ GJ/ton of $\text{CO}_2 = 10$ EJ/Gt of gross CO_2 extraction

511 Note that 1 exa (10^{18}) = 1 giga (10^9) * 1 giga (10^9).

512
 513 Thus, a capped 20 Gt CO_2 extracted (in gross term) in 2100 in our base case would require 200 EJ per year,
 514 consisting of a major component of the energy landscape. For context, global PE in 2013 is about 567 EJ/year.

515
 516 Next, $f_i(t)$ = fossil fuel fraction of the PE = $E_{11}(t)$ (36)

517 And $\rho_i(t)$ is the carbon intensity which can vary in time.

518
 519 Lastly, we formulate the response times required in Eqn. 25:

520
 521
$$\tau_i(t) = \tau_i^0 * e^{-C_0|T(t)-\alpha_i|} ; \quad \text{if } \tau_i(t) < 1 \text{ year, set } \tau_i(t) = 1 \text{ year} \quad (37)$$

522
 523 The constants in Eqn. 37 are set as:

524 $C_0 = 1 \text{ year}^{-1}$ (38)

525 $\tau_1^0 = 10$ years; $\alpha_1 = 1$ °C (39)

526 $\tau_2^0 = 10$ years; $\alpha_2 = 1.5$ °C (40)

527 $\tau_3^0 = 10$ years; $\alpha_3 = 2$ °C (41)

528

529
530
531
532

Part 2
Sensitivity studies conducted with ISEEC
including 1 Supporting Table and 12 Supporting Figures

533 **Table S3. Sensitivity studies for Energy-Climate Interactions. R_1.5C is Share of Renewable at 1.5°C**
534 **warming. The fully coupled version of ISEEC includes the following: warming-dependent response times;**
535 **mitigation of SLCPs and aerosols emitted by fossil fuels; Atmospheric Carbon Extraction driven by warming.**
536 **The three entries under the second column (“CO₂ Net Emission”) are peak emission amount (and year of**
537 **peaking); year of reaching net-zero emission; and cumulative net emission (from 2015 to 2100).**
538

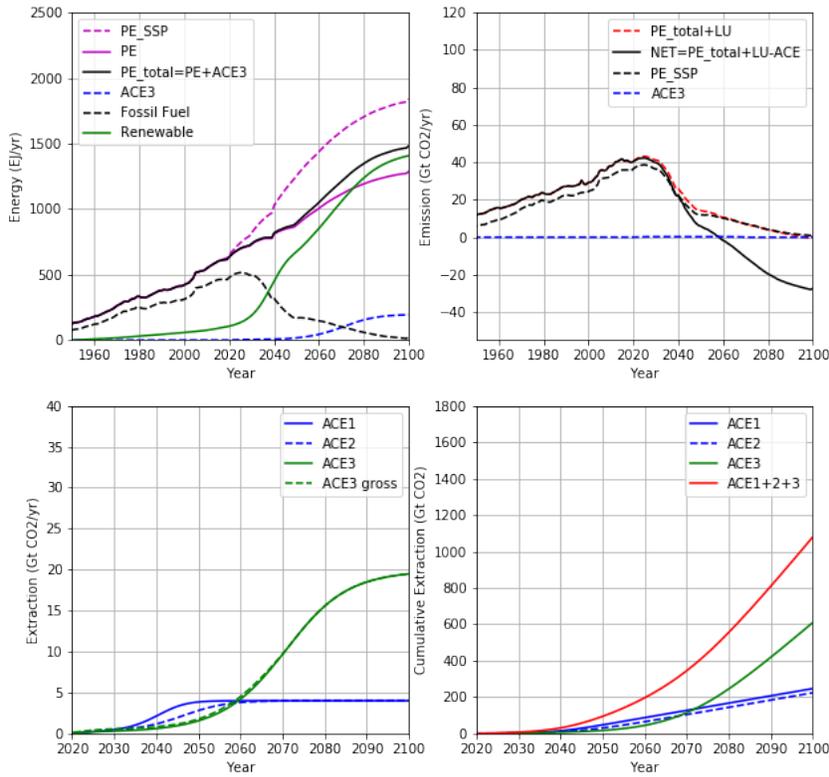
Case Number and Case Name	CO ₂ Net Emission	Peak CO ₂ Concentration (Year)	Peak Warming (Year)	2100 Warming	R_1.5C and ACE (from 2015 to 2100)	Details
1. ISEEC-Fully Coupled	42 Gt (2025); 2058; 350 Gt	435 ppm (2047)	2.3°C (2075)	2.2°C	20% 1100 Gt	Base model with all the energy-climate interactions. Fig. S2-1.
1.b ISEEC-Fully Coupled	42 Gt (2025); 2058; 300 Gt	430 ppm (2045)	2.2°C (2075)	2.1°C	20% 1050 Gt	Base model but a smaller b ₁ of 20 years. Fig. S2-11.
2.a ISEEC-Partially Decoupled	42 Gt (2030); n/a; 2460 Gt	480 ppm (2040)	>3.5°C (>2100)	3.5°C	13% 1050 Gt	Same as 1, but without warming dependent response times; fixed at 2015 values. Fig. S2-2.
2.b ISEEC-Fully Decoupled	60 Gt (2050); n/a; 4050 Gt	590 ppm (2100)	>4.6°C (>2100)	4.6°C	11% 1050 Gt	Same as 2.a, but also without warming dependent energy intensity, fixed at 1.0. Fig. S2-10.
3. Case 1 with faster response times	42 Gt (2021); 2050; 60 Gt	425 ppm (2040)	2.1°C (2075)	2°C	45% 1000 Gt	Beginning 2016, response times were estimated using projected warming 20 years into the future. Fig. S2-3.

4. Case 1 with a boost in initial investment	41 Gt (2020); 2045; -100 Gt	415 ppm (2038)	2.0°C (2090)	1.9°C	55% 850 Gt	Beginning 2016, increase start-up investment from 0.1%/year to 2%/year. Fig. S2-4 and Fig. S2-5.
5. Cases 3+ 4 + mitigation of all SLCPs	41 Gt (2020); 2038; -25 Gt	415 ppm (2029)	1.6°C (2040)	1.4°C	70% 700 Gt	Mitigation of non-fossil fuel SLCPs, in addition to fossil fuel. Fig. S2-6.
6. Case 1+ without ACE	45 Gt (2030) 2100; 1420 Gt	440 ppm (2045)	2.5°C (2100)	2.5°C	22% 0 Gt	Fig. S2-7.
7. Case 6+ without fossil fuel related SLCP mitigation.	45 Gt (2030) 2100; 1390 Gt	440 ppm (2045)	3.1°C (2100)	3.1°C	22% 0 Gt	Fig. S2-8.
8. Case 6+ without improvement of energy intensity	50 Gt (2030) 2100; 1770 Gt	460 ppm (2050)	2.7°C (2100)	2.7°C	22% 0 Gt	Energy intensity ratio set to 1.0. Fig. S2-9.
9. Case 1 + mitigation of all SLCPs	42 Gt (2021); 2068; 1040 Gt	450 ppm (2050)	1.8°C (2050)	1.8°C	45% 800 Gt	Mitigation of non-fossil fuel SLCPs, in addition to fossil fuel. Fig. S2-12.

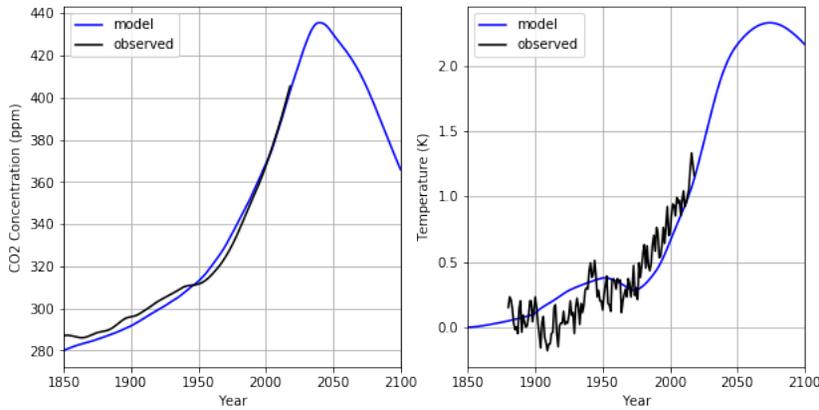
539

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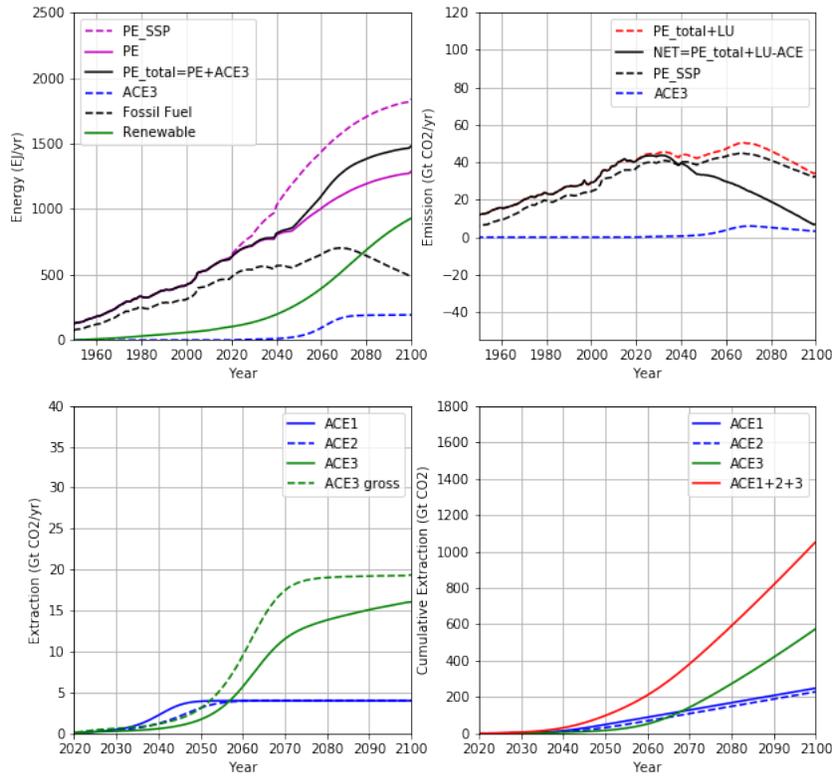
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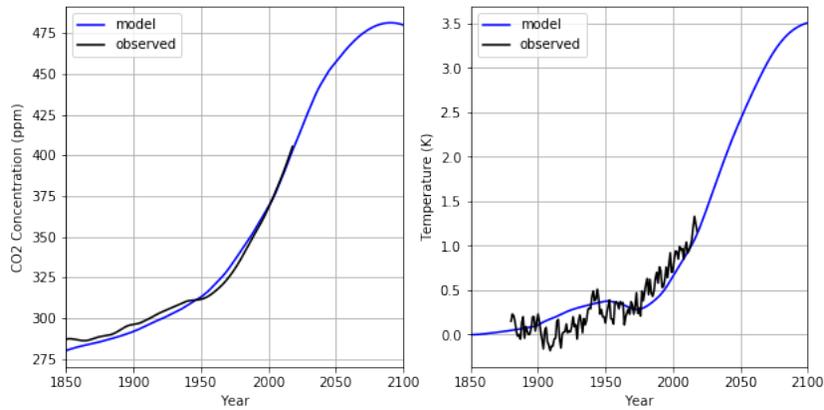
545 **Fig. S2-1. The base version of ISEEC (fully coupled). All response times are temperature dependent. SLCP**
546 **mitigation is coupled with fossil fuel use. Same as in Fig. 4 top panels.**

547

548



549

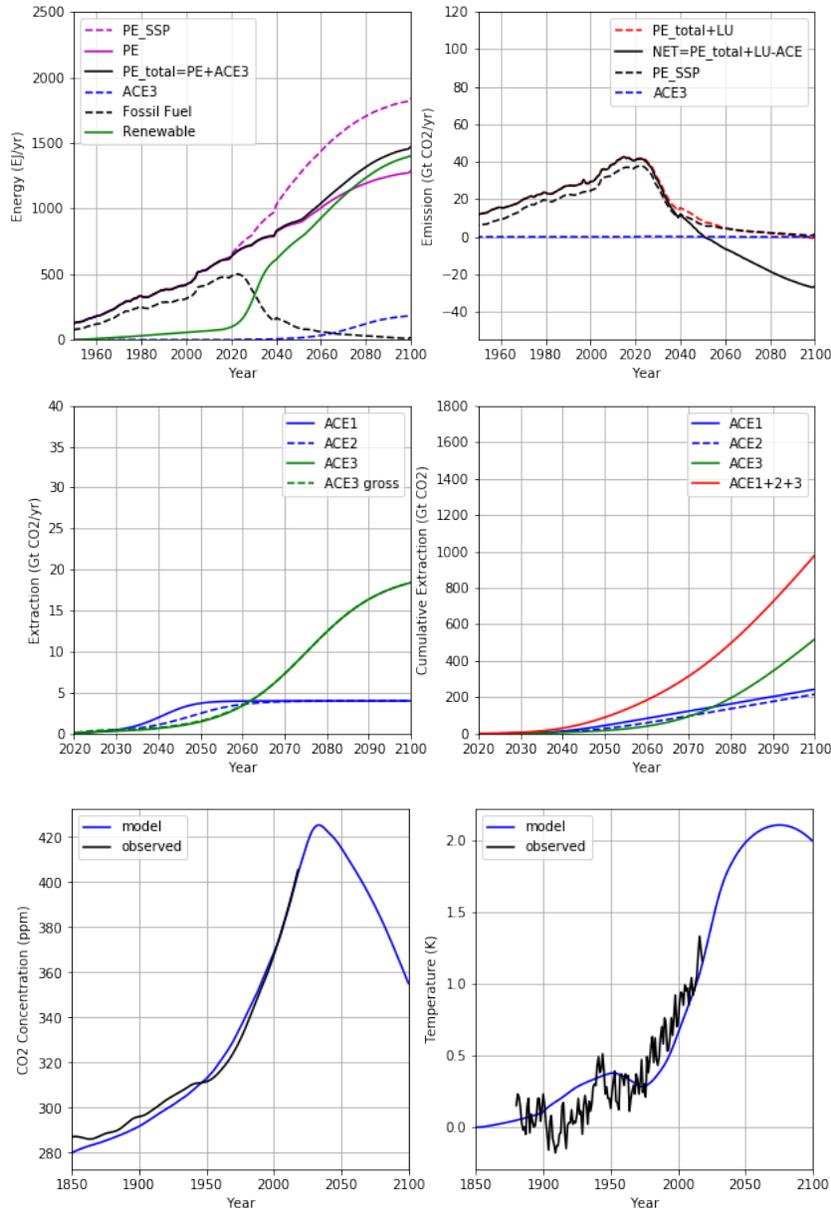


550

551

552 **Fig. S2-2. ISEEC Partially Decoupled. That is, the response times are fixed at their 2015 levels. ACE3 in the**
553 **top-right panel of “Emission” is the ACE3-related emission, which would offset the gross extraction amount**
554 **(dashed green line in “Extraction” panel) thus the net ACE3 extraction (solid green in “Extraction” panel) is**
555 **smaller. “ACE3” (solid green line) in the “Cumulative Extraction” panel refers to the net amount of**
556 **extraction (i.e., gross minus offset).**

557



558

559

560

561 **Fig. S2-3. Same as the base case, but with a quicker time constant reduction based on anticipated warming 20**

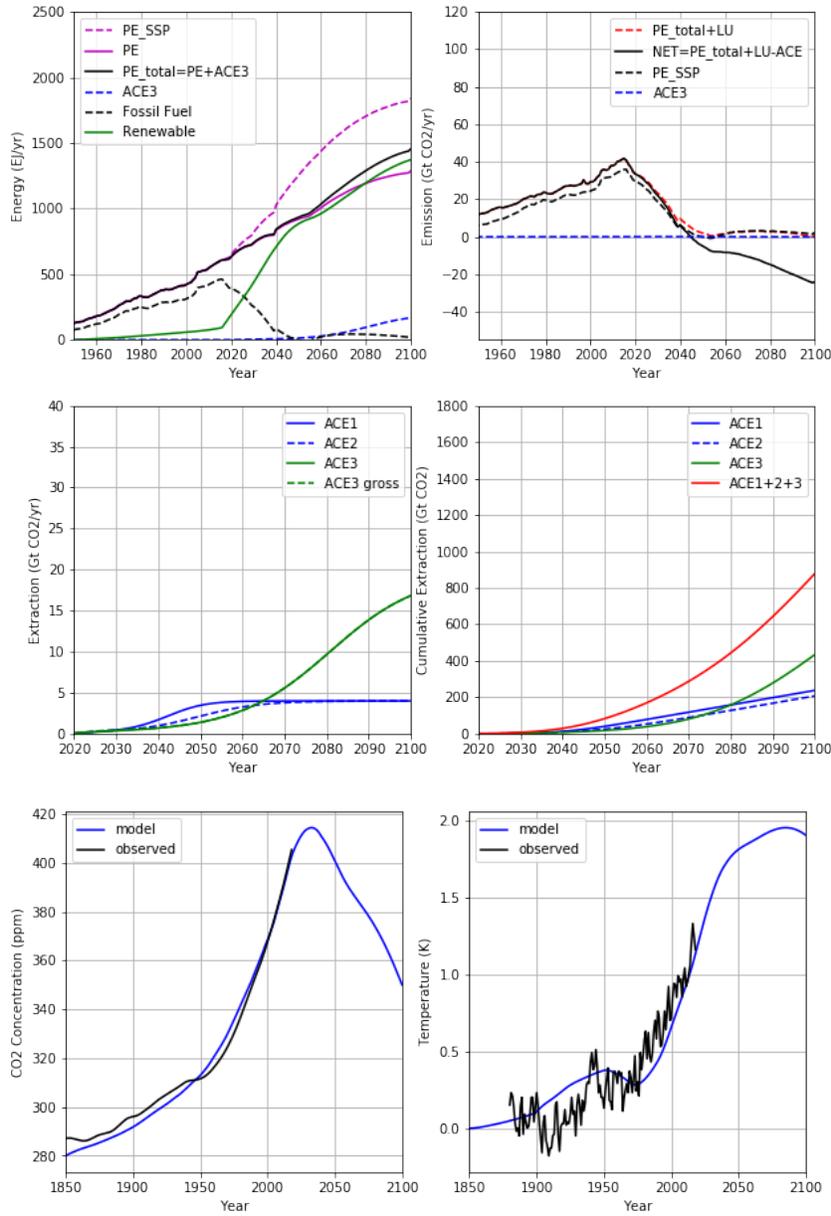
562 **years ahead (i.e., $\sim 0.6^\circ\text{C}$ warmer). We replaced the temperature in the response time $\tau_{ij}(t)$ with $T(t) =$**

563 **$T'(t) + 0.6^\circ\text{C}$, where $T(t)$ is the temperature inserted in the equations for τ_{ij} and $T'(t)$ is the temperature**

564 **simulated by the NSM. The addition of 0.6°C is equivalent to the additional warming over the next 20 years**

565 **because the projected warming rate is about $0.3^\circ\text{C}/\text{decade}$.**

566



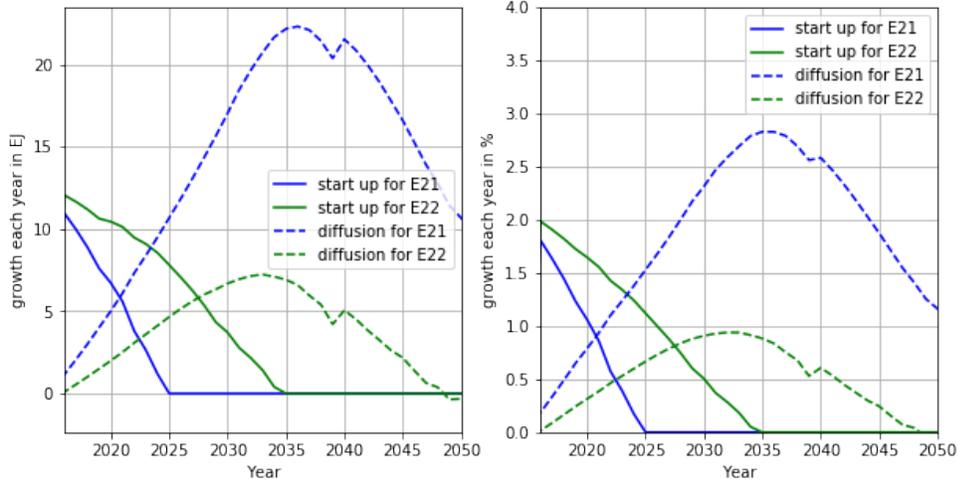
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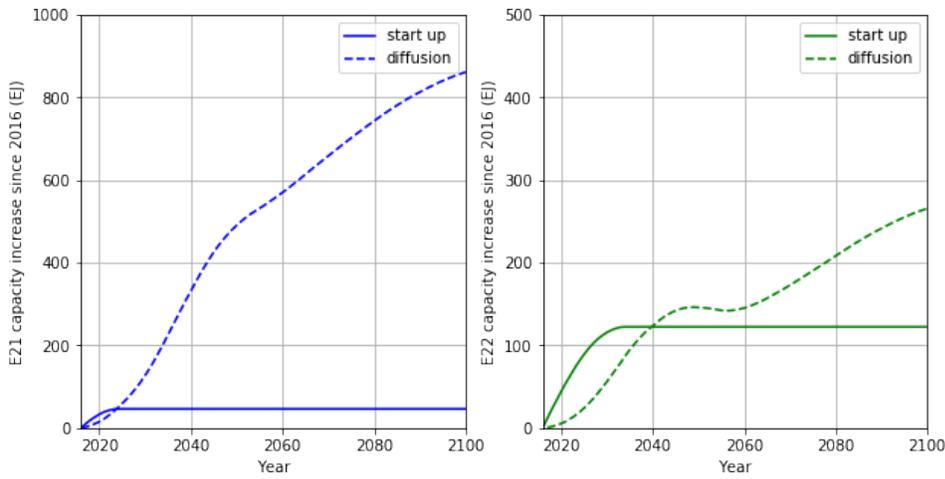
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570 **Fig. S2-4. Same as the base case, but the initial startup terms for E_{21} and E_{22} are increased to 2%/year**
 571 **beginning 2016.**

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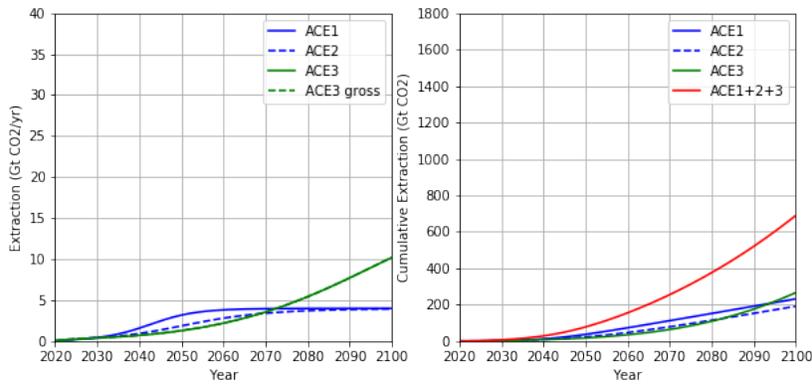
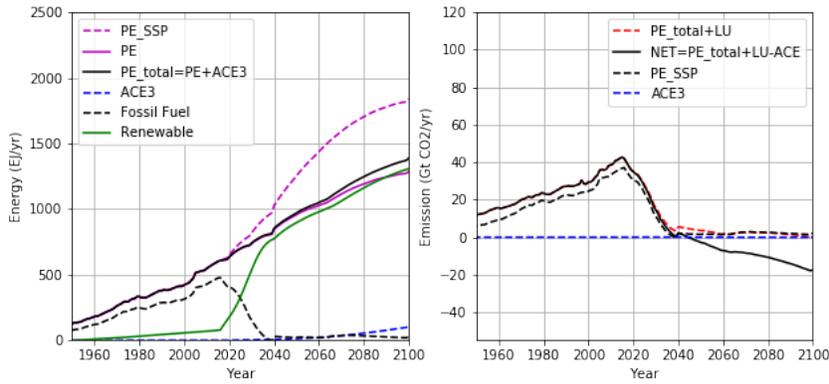
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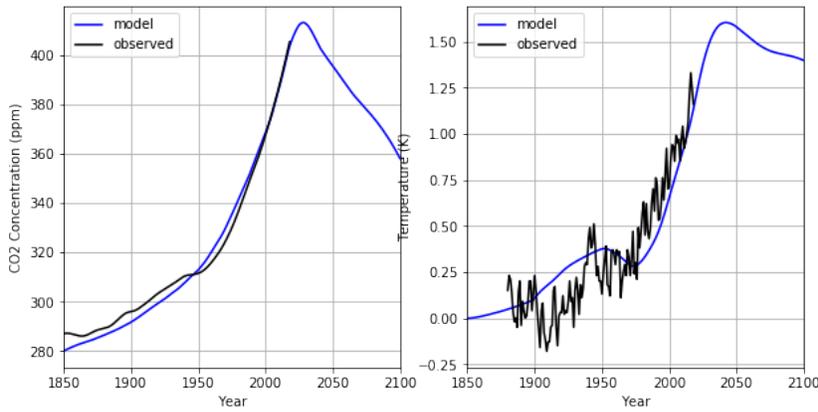
576 **Fig. S2-5. The breakdown of start-up term and diffusion term (in Eqn. 1) as in Case 4 (Fig. S2-4): initial**
 577 **startup terms of 2%/year beginning 2016.**

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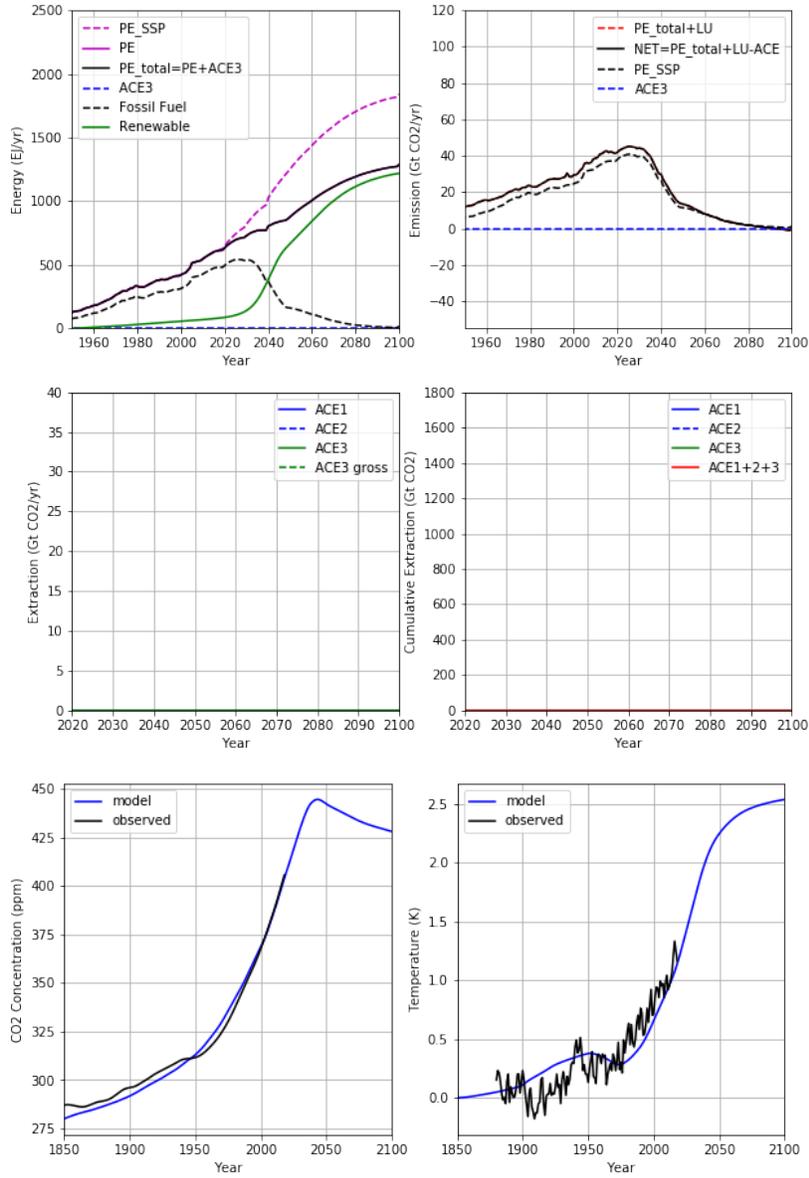


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Fig. S2-6. Full SLCP mitigation, but also with faster reduction of response time due to anticipated higher warming, and a 2%/year initial start-up investment. Also shown in Fig. 5.



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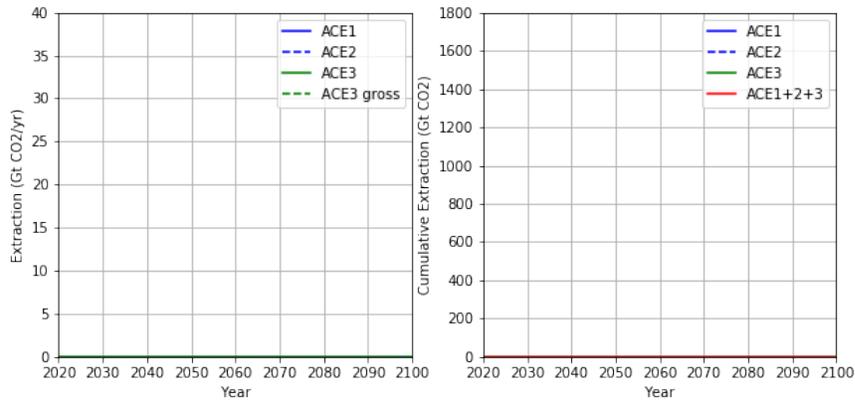
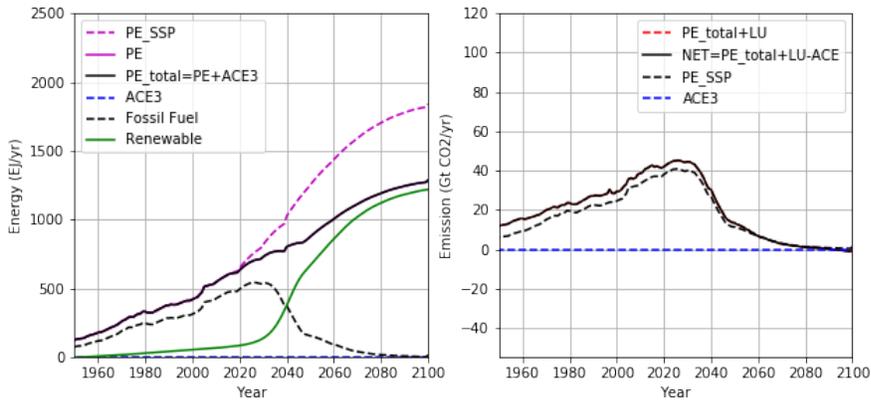
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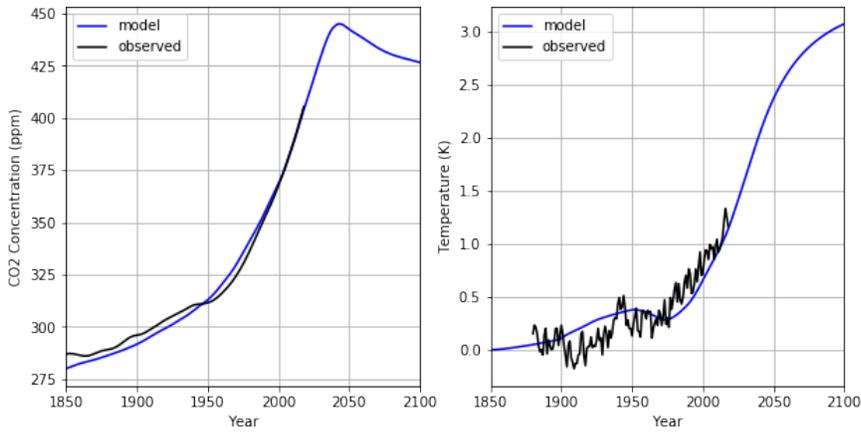
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Fig. S2-7. Same as the base model but without ACE.

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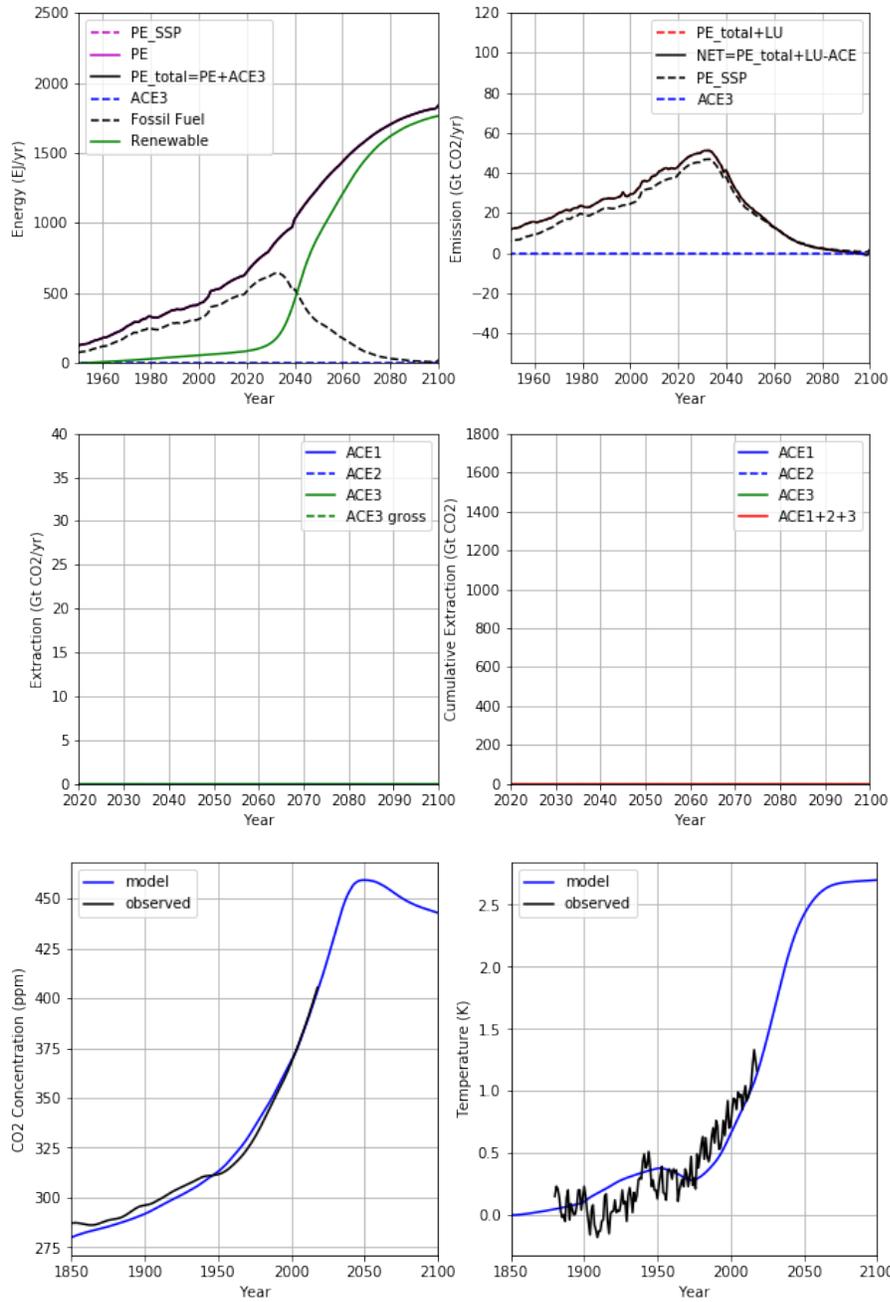
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Fig. S2-8. Same as Case 6, but also without mitigating fossil fuel SLCPs.



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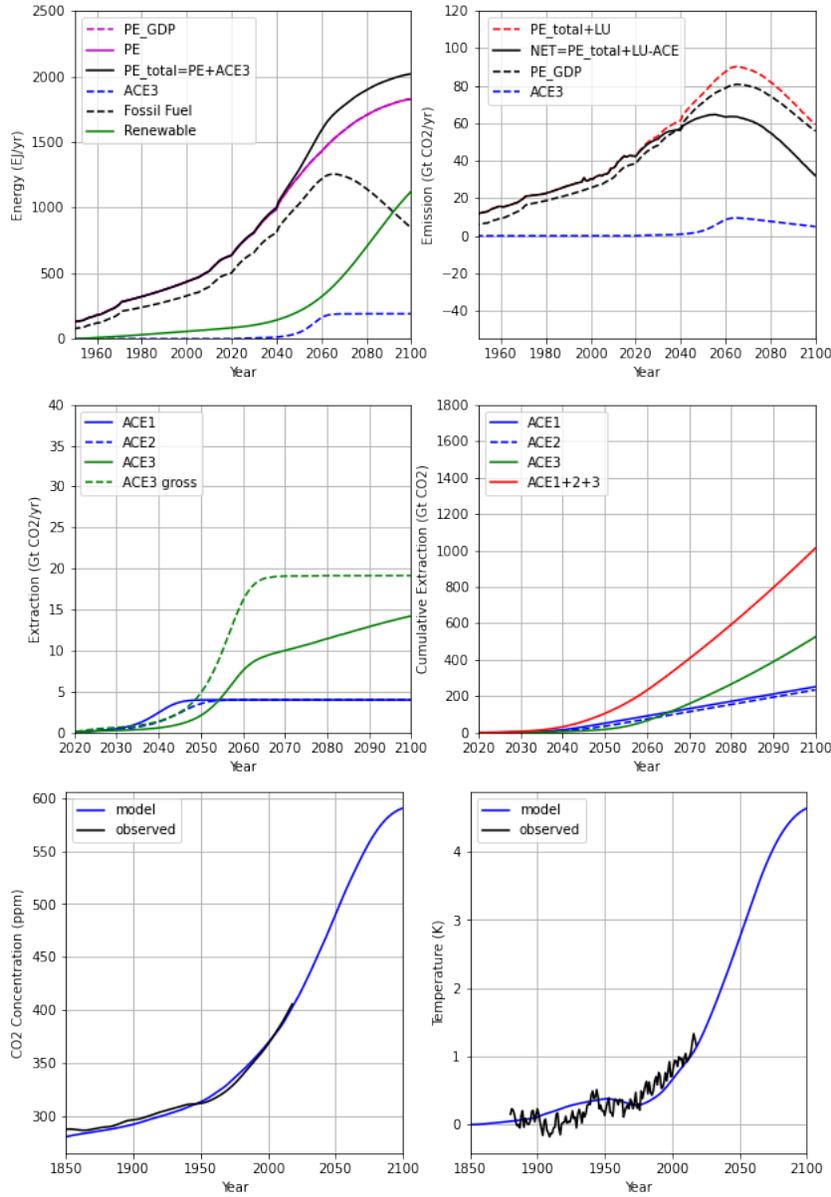
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Fig. S2-9. Same as Case 6, but with the energy intensity ratio set to 1.0 throughout the 21st century.



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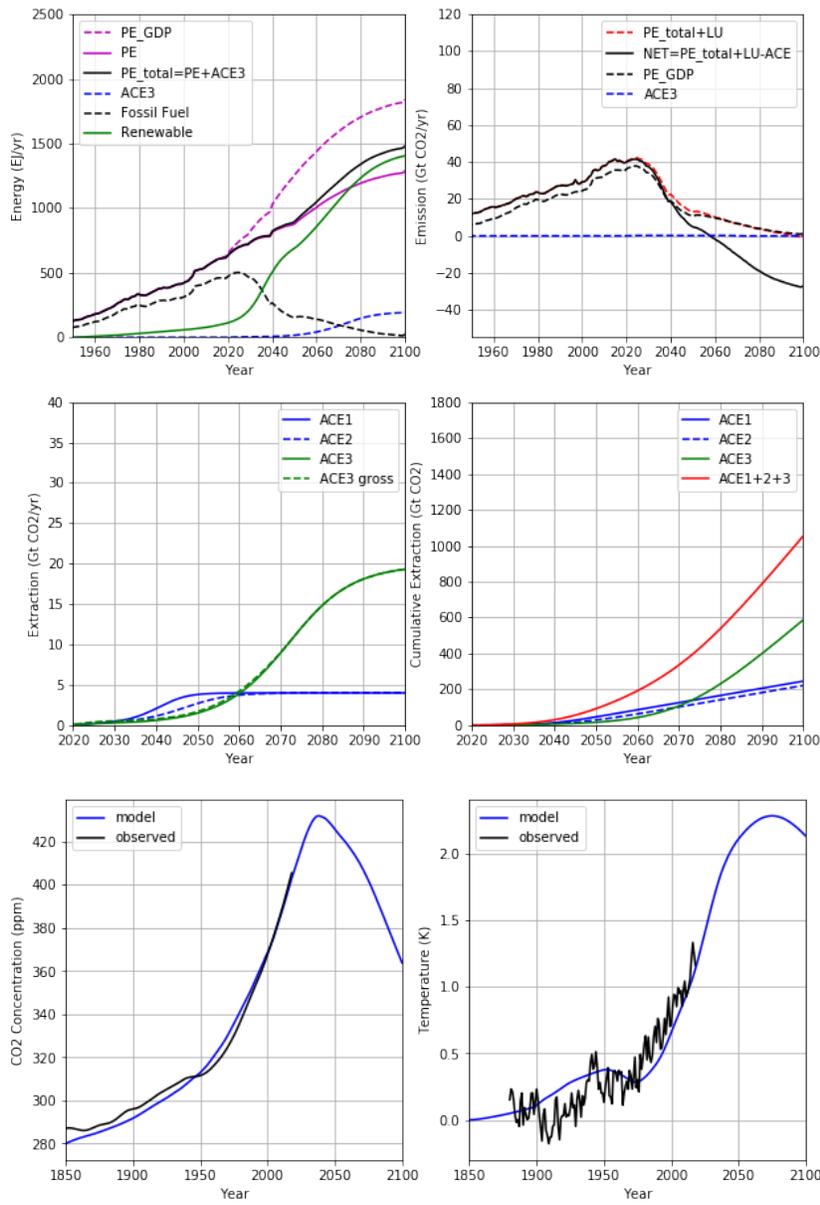
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Fig. S2-10. Case 2.b, also shown in Fig. 4 bottom panels.

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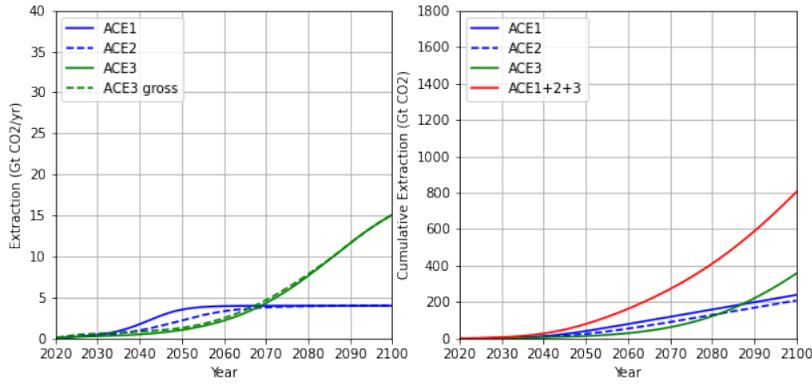
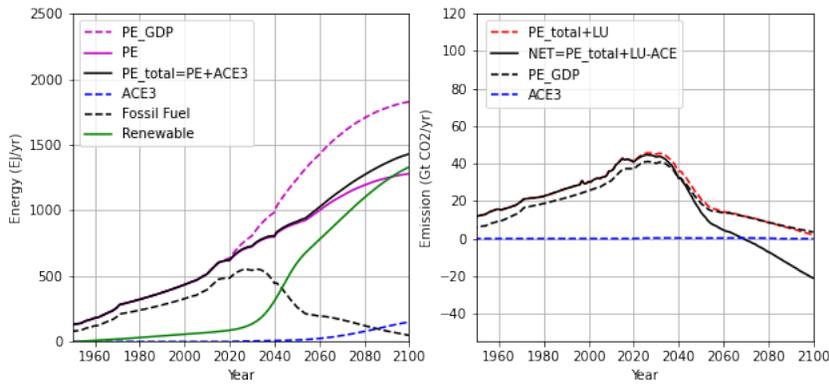
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612 **Fig. S2-11. The base case of ISEEC (fully Coupled) but with $b_1=20$ years as tested in Fig. S2-3b. Note that**

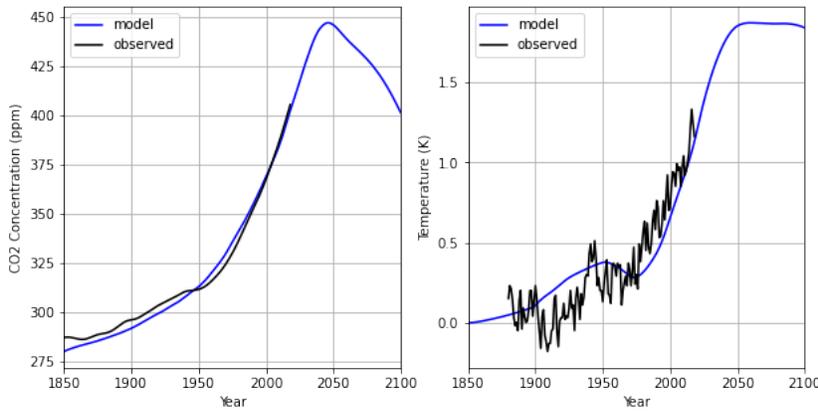
613 **because of the smaller response time, the end of century warming is lowered by $\sim 0.2^\circ\text{C}$ to 2.1°C .**

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Fig. S2-12. Base version of the model, but including mitigation of non-fossil fuel SLCPs, in addition to fossil fuel sources. Also shown in Fig. 5.

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